

# Modelling 100 percent renewable electricity

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(Thanks to Golbon Zakeri, Corey Kok and Ziming Guan.)

# What is EPOC?

- Electric Power Optimization Centre (EPOC) founded in 2002 at UoA.
- Electricity modelling “Winter” workshops held every year since 2002. See [www.epoc.org.nz/workshops.html](http://www.epoc.org.nz/workshops.html)
- EPOC modelling systems in this talk:
  - **DOASA**: hydro-thermal optimization model of NZ electricity system (C++/Gurobi)
  - **vSPD**: Electricity Authority version of SPD (GAMS/Cplex)
  - **HydrovSPD**: vSPD with hydro river chains modelled over 48 periods (GAMS/Cplex)
  - **GEMstone**: GEM with stochastic optimization (GAMS/Conopt)
  - **CRAGE**: Competitive Risk-Averse Generation Expansion (GAMS/PATH)

# Motivation for this talk

- Electricity generation worldwide emits greenhouse gases so to reduce greenhouse gases one can reduce **nonrenewable** electricity generation.
- Why not reduce nonrenewable electricity generation to zero?
- **Aspiration**: a 100% renewable electricity system for NZ.
- What are models good for?
  - **GEMstone** reveals the implications of the aspiration;
  - **GEMstone** determines a system investment plan to achieve the aspiration or get close to it;
  - **DOASA/HydrovSPD** tests the robustness of the investment in dry winters;
  - **CRAGE** determines how to get close to the system optimum using incentives.

# Implications: what does 100% renewable mean?

- Shutdown all thermal plant? Won't this be expensive?
- Keep some thermal plant, but use sparingly (in a low-hydrology year)?
- Control GHG emissions from electricity generation to below an accepted threshold?
- Is this a constraint on average, or almost always, or with high probability?
- Planning for future years involves uncertainty, so we need stochastic models.
  - we need to know if capacity plans affect security of supply?

# Competitive markets and expansion

- How do we get companies to follow the system plan?
- **Second Welfare Theorem**: a system plan that minimizes the expected cost of meeting future demand yields energy prices in each state of the world. Each investment action in the plan is optimal for its investor when evaluated using these energy prices. It is a **Walrasian (partial) equilibrium**.
- Then, why do electricity companies always do something different from the GEMstone system plan?

# Summary

- 1 Introduction
- 2 GEMstone
- 3 DOASA/HydrovSPD
- 4 CRAGE
- 5 Conclusions

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# GEMstone for a single node

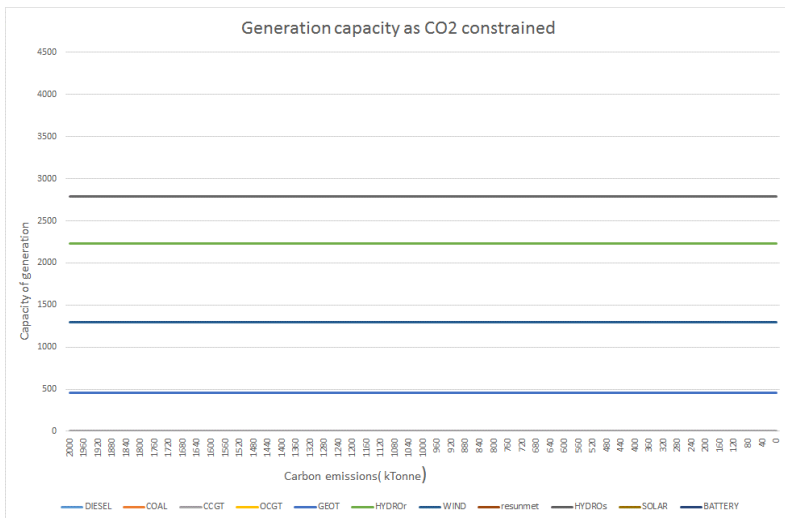
Plant  $k$  has current capacity  $U_k$ , expansion  $x_k$  at capital cost  $K_k$  per MW, maintenance cost  $L_k$  per MW, and SRMC  $C_k$ . Minimize fixed and **expected** variable costs.

$$\begin{aligned}
 \text{P: } \quad \min \psi &= \sum_{k \in \mathcal{K}} (K_k x_k + L_k z_k) + \mathbb{E}_\omega [Z(\omega)] \\
 \text{s.t. } \quad Z(\omega) &= \sum_{b \in \mathcal{B}} T(b) (\sum_k C_k y_k(\omega, b) + Vq(\omega, b)) \\
 x_k &\leq u_k, & k \in \mathcal{K} \\
 z_k &\leq x_k + U_k, & k \in \mathcal{K} \\
 y_k(\omega, b) &\leq \mu_k(\omega, b) z_k, & b \in \mathcal{B}, \omega \in \Omega, k \in \mathcal{K}, \\
 \sum_{b \in \mathcal{B}} T(b) y_k(\omega, b) &\leq \nu_k(\omega) \sum_{b \in \mathcal{B}} T(b) z_k, & b \in \mathcal{B}, \omega \in \Omega, \\
 q(\omega, b) &\leq d(\omega, b), & b \in \mathcal{B}, \omega \in \Omega, \\
 d(b) &\leq \sum_{k \in \mathcal{K}} y_k(\omega, b) + q(\omega, b), & b \in \mathcal{B}, \omega \in \Omega.
 \end{aligned}$$

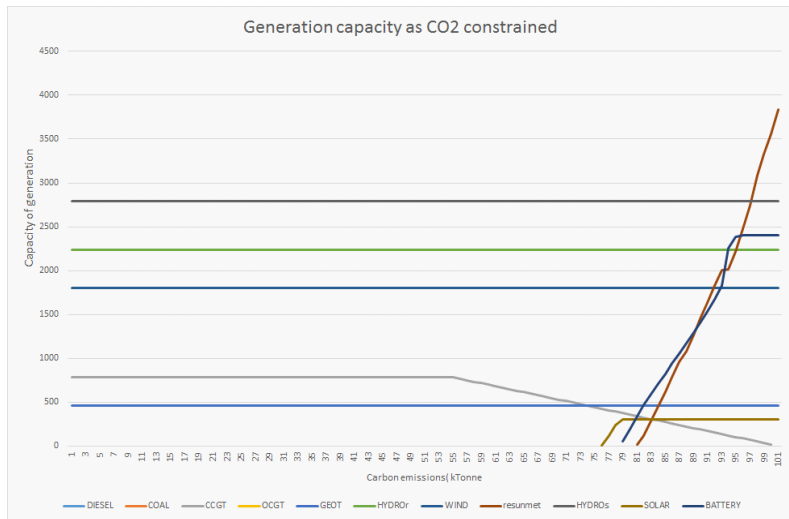




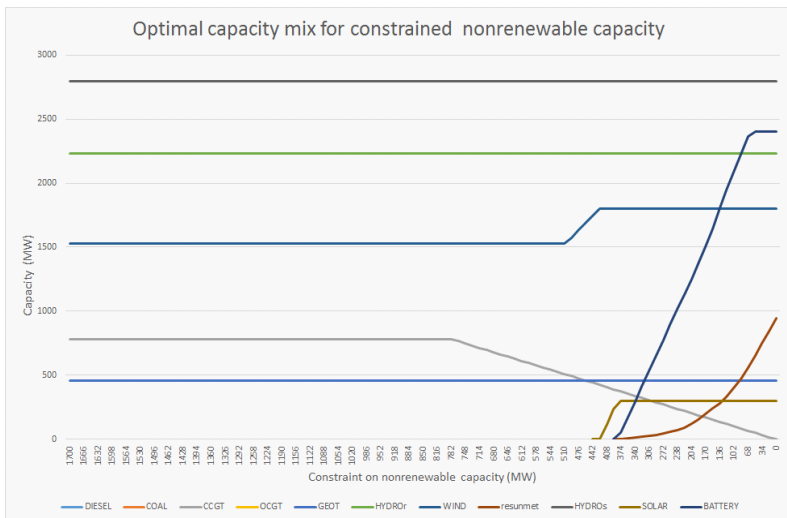
# Deterministic result: 100% renewable in a wet year (2016)



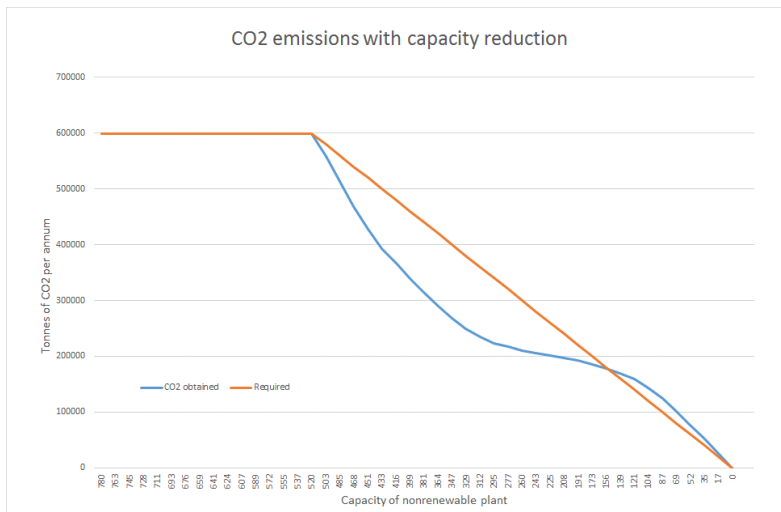
# Deterministic result: 100% renewable in a dry year (2008)



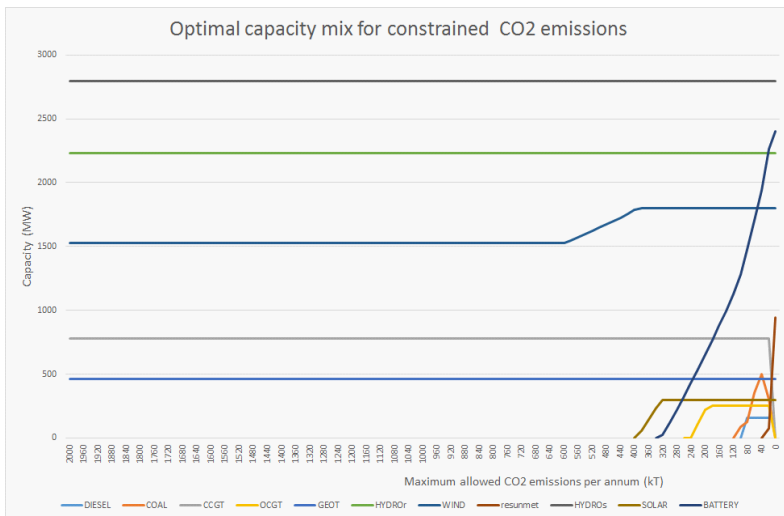
# GEMstone result: eliminate nonrenewable capacity?



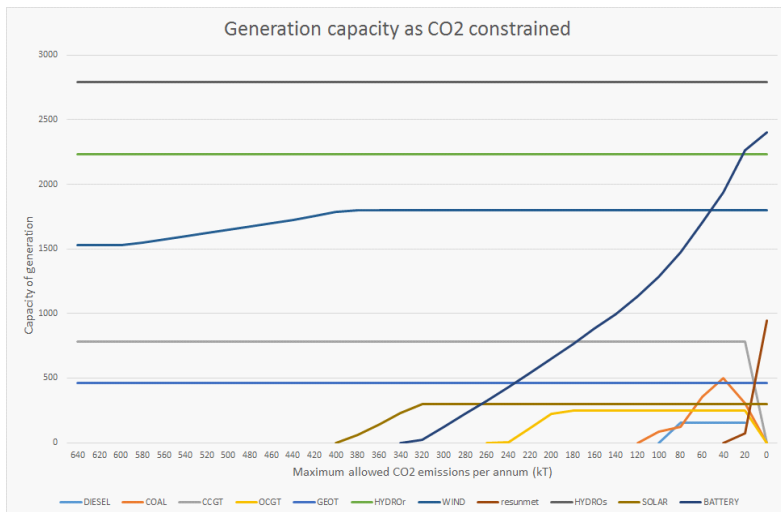
# Emissions if eliminate nonrenewable capacity



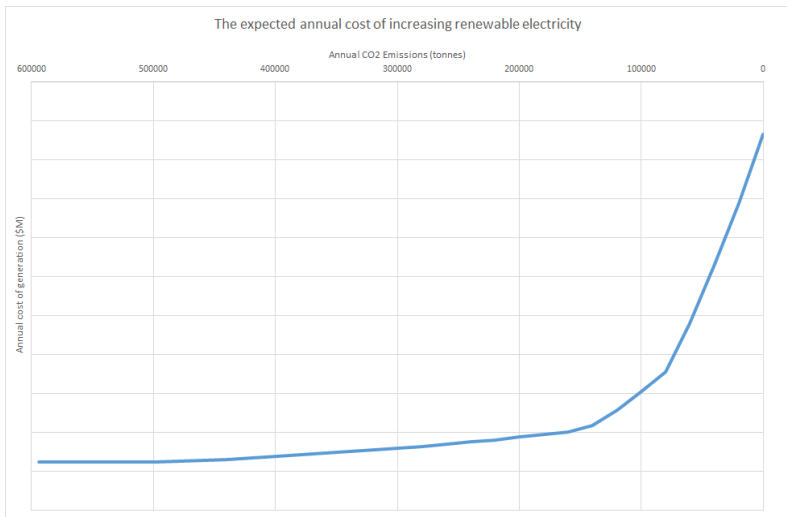
# GEMstone result: eliminate average emissions



# GEMstone result: eliminate average emissions (detail)

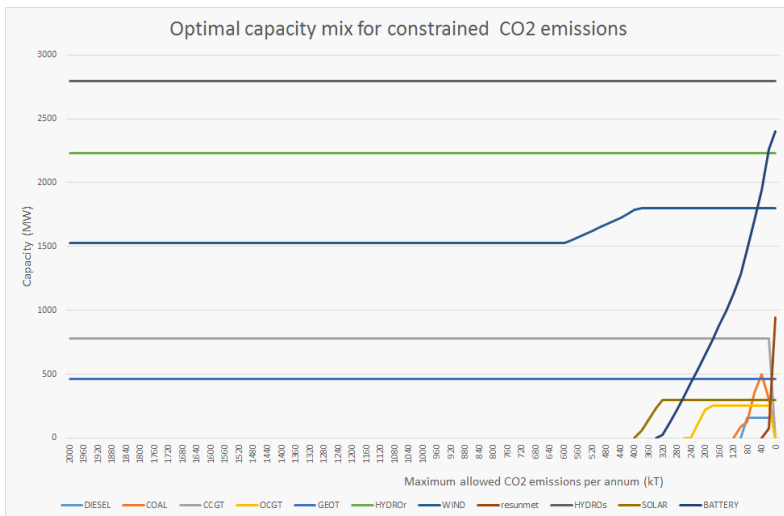


# The expected cost of reducing average electricity emissions

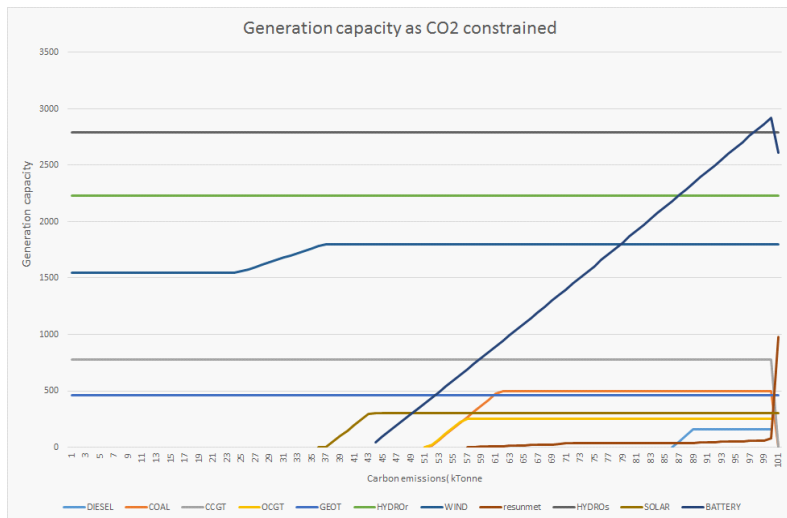




# GEMstone result: eliminate average emissions



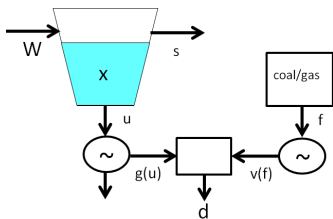
# GEMstone result: eliminate emissions almost surely



# Summary

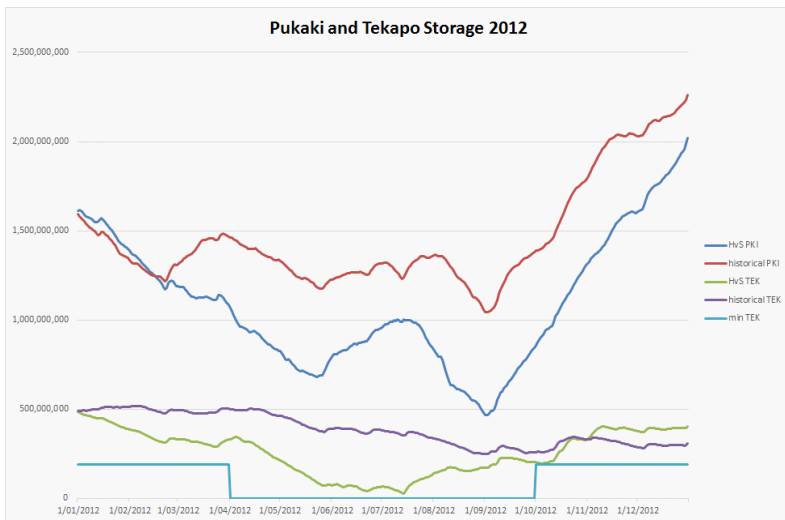
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# DOASA/HydrovSPD

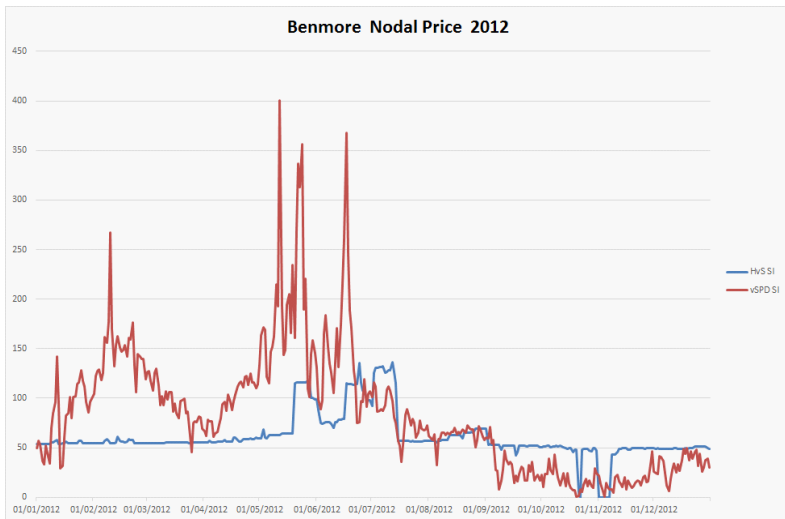


- Use water or thermal plant generation?
- DOASA computes an **expected marginal water value** for stored water under perfect competition.
- Requires solution of massive scale stochastic optimization using SDDP algorithm.
- Water is not released if its expected marginal value exceeds SRMC of thermal plant.
- Policy simulated in HydrovSPD.

# Outcomes from DOASA/HydrovSPD



# Outcomes from DOASA/HydrovSPD



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# Risk and competition

- Why do electricity companies do something different from the GEMstone system plan?
- Companies expand capacity using debt and equity. Banks dislike **risk**, so expansion plans aim to reduce risk.
- **CRAGE** computes the risked partial equilibrium of competing companies.
- System expansion plans (**GEMstone**) can pool the risks of different cost streams, so risk-averse system optimization gives less risk. Risk-averse companies looking at only their profit streams will not do what the system deems optimal.
- **CRAGE** equilibrium  $\neq$  **GEMstone** optimum with social risk measure.



# CRAGE

Simultaneous solution of

$$P(a): \quad \min \psi = \sum_{k \in \mathcal{K}} (K_k x_k^a + L_k z_k^a) + \rho_a [Z^a(\omega)]$$

$$\text{s.t.} \quad Z^a(\omega) = \sum_{b \in \mathcal{B}} T(b) (\sum_k C_k y_k^a(\omega, b) + Vq^a(\omega, b) - \pi(\omega, b) (\sum_{k \in \mathcal{K}} y_k^a(\omega, b) + q^a(\omega, b)))$$

$$x_k^a \leq u_k^a, \quad k \in \mathcal{K}$$

$$z_k^a \leq x_k^a + U_k^a, \quad k \in \mathcal{K}$$

$$y_k^a(\omega, b) \leq \mu_k(\omega, b) z_k^a, \quad b \in \mathcal{B}, \omega \in \Omega, k \in \mathcal{K},$$

$$\sum_{b \in \mathcal{B}} T(b) y_k^a(\omega, b) \leq v_k(\omega) \sum_{b \in \mathcal{B}} T(b) z_k^a, \quad b \in \mathcal{B}, \omega \in \Omega,$$

$$q^a(\omega, b) \leq d(\omega, b), \quad b \in \mathcal{B}, \omega \in \Omega,$$

$$0 \leq \sum_{k \in \mathcal{K}} y_k^a(\omega, b) + q^a(\omega, b) - d(b) \perp \pi(\omega, b) \geq 0 \perp \pi(\omega, b) \geq 0.$$

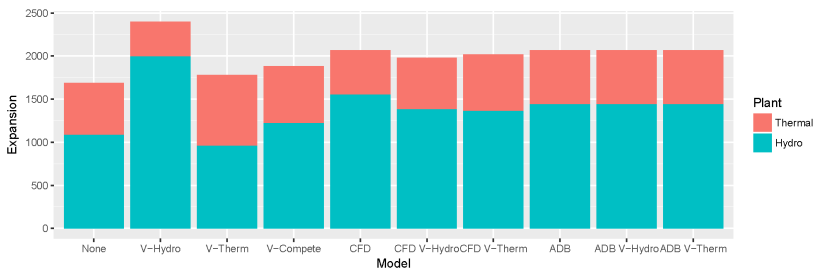
# Risk trading can recover system optimum

- **Contracts** for trading risk enable companies to enjoy pooled risk.
- Perfectly competitive markets can be **inefficient** if such contracts are missing.
- Example: Meridian-Genesis swaption contract enables more efficient operation of thermal and hydro plant by decreasing risk for both parties.
- Theorem (PFW, 2016; FP, 2018): If markets for risk (using **dynamic coherent risk measures**) are **complete** then a perfectly competitive (risk-averse) equilibrium corresponds to a risk-averse **social optimum** using a social risk measure.
- **CRAGE** equilibrium with contracts = **GEMstone** risk-averse optimum.

# Modelling implications

- **CRAGE** model can predict competitive equilibrium investments in incomplete markets.
- **GEMstone** risk-averse optimum can provide a benchmark for complete market.
- The added value of adding **contracts** for trading risk can be identified from the difference between these solutions.

# Outcomes



Different expansion plans arising from incomplete markets for risk.  
(Source Corey Kok PhD thesis).

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- What are EPOC models good for?
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  - **DOASA/HydrovSPD** tests the robustness of the investment in dry winters;
  - **CRAGE** determines how to get close to the system optimum using incentives.
- DOASA made available as EMI-DOASA on the EA EMI site.
- All the EPOC models are currently calibrated to the New Zealand electricity system and ready to apply.

# The End

# THE END

## References

- Ferris, M.C., Philpott, A.B., Dynamic risked equilibrium, *EPOC technical report*, 2018.
- Philpott, A.B., Ferris, M.C. and Wets, R.J-B., Equilibrium, uncertainty and risk in hydrothermal electricity systems, *Mathematical Programming B*, 157,2, 483-513, 2016.
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- Kok, C., Philpott, A.B. and Zakeri, G., Value of transmission capacity in electricity markets with risk averse agents, *EPOC technical report*, 2018.

All references and this talk can be downloaded from  
[www.epoc.org.nz](http://www.epoc.org.nz)