

Generation Expansion Model (GEM)

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Outline

- Overview of model
 - Basics
 - Objective function
 - Constraints
- Some key aspects
 - Build decision
 - Treatment of transmission losses
 - Security constraints
 - One or two contentious topics
 - Solution strategies
- Illustrative outputs
- What next?
- Further information

Overview of model

- Basics
- GEM is a long term capacity expansion planning model
- Formulated as a mixed integer programming problem (MIP)
- Coded using GAMS and solved with CPLEX
- Input data compiled in an Excel spreadsheet
- Output files generated as tab or comma delimited text files
- Matlab scripts used to process output files
- Publicly available
- Objective function
- Minimise discounted costs
 - Capital expenditure, fixed and variable operating costs
 - Penalties on potential infeasibilities

Overview of model – cont'd

- Constraints
- Compute costs (including HVDC charge), 3 constraints
- Build decision and capacity balance, 5 constraints (see below)
- 3 accounting equations – generation by quarter and year, and fuel by year
- Energy balance constraint
- Determine losses (see below)
- 3 security constraints (see below)
- 6 technical operating constraints – minimum and maximum capacity factors, minimum utilisation by technology type, limits on fuel availability, e.g. gas, and limit on energy from a single fuel type, e.g. wind, and hydro generation limited by inflows.
- 2 renewables targets constraints – energy and capacity
- 3 constraints to control operation of pumped hydro schemes

Build decision

** Ensure new station is fully built only once, if at all.*

bldGenOnce(posbuild(s))..

SUM(validbldyr(s,y), GENBLDINT(s,y)\$intbld(s) + GENBLDCONT(s,y)\$contbld(s))
=1= 1;

** If new 'integer' station is built, ensure it doesn't exceed nameplate capacity.*

buildCapInt(s,y)\$ (posbuild(s) * intbld(s) * validbldyr(s,y))..

BUILD(s,y) =e= GENBLDINT(s,y) * nameplate(s) ;

** If new 'continuous' station is built, ensure it doesn't exceed nameplate capacity.*

buildCapCont(s,y)\$ (posbuild(s) * contbld(s) * validbldyr(s,y))..

BUILD(s,y) =e= GENBLDCONT(s,y) * nameplate(s) ;

** Restrict aggregate new capacity built in a single year to be less than AnnMW.*

AnnNewMWcap(vY(y))\$ (%AnnMW% <= 1000)..

SUM(s\$ (posbuild(s) * validbldyr(s,y)), BUILD(s,y)) =1= %AnnMW% ;

** Keep track of capacity in each year.*

balance_capacity(s,vY(y))..

CAPACITY(s,y) =e= InitCap(s)\$firstYr(y) + CAPACITY(s,y-1)\$vYx1(y) + BUILD(s,y) -
RETIRE(s,y) ;

Losses – piecewise linear approximation

- A simple convex formulation works well, as losses are implicitly costly
- User selects number of line segments to use – currently using 5

** Piecewise linear transmission losses.*

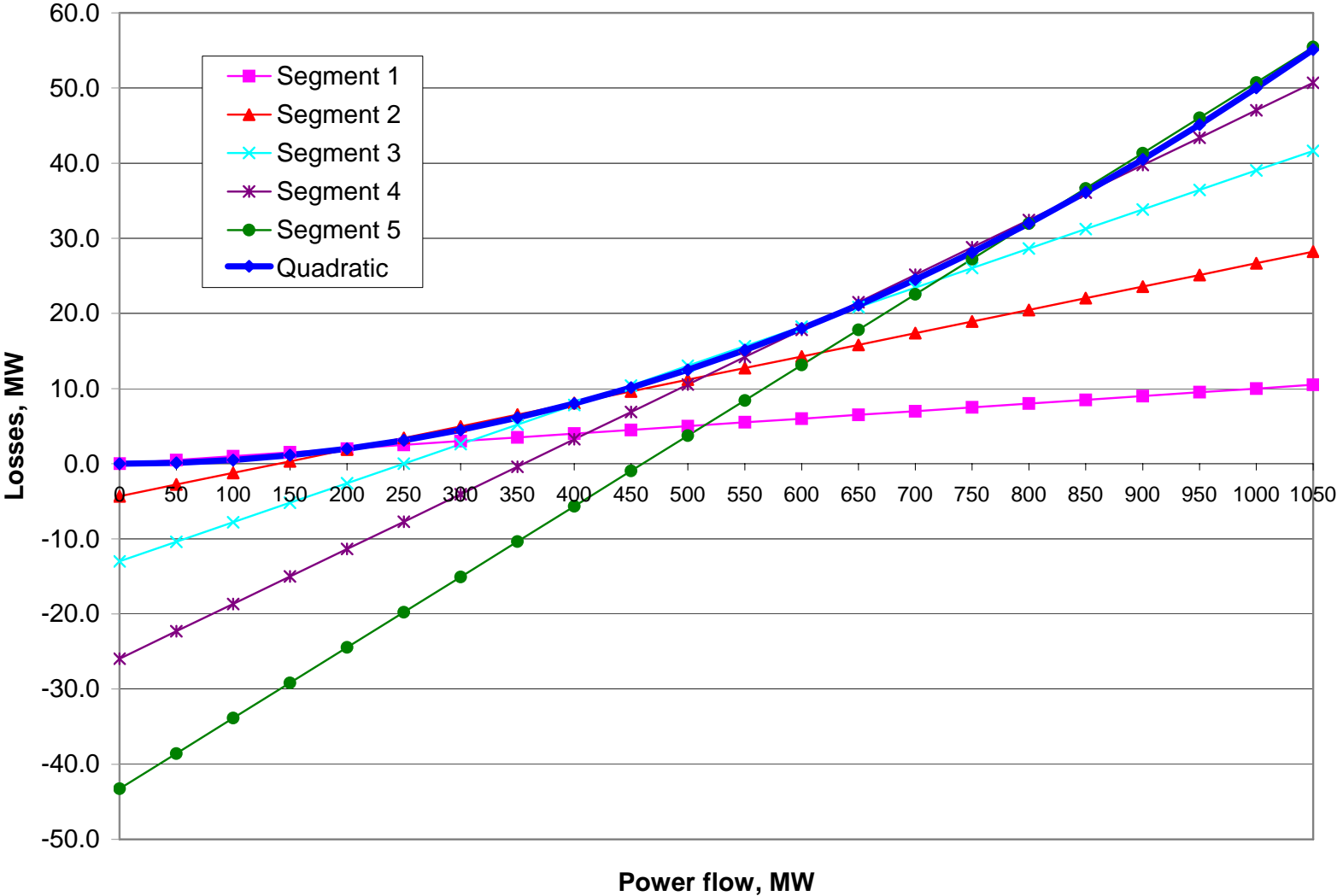
```
boundTxloss(ild,ild1,vY(y),t,blk,nsegment(n))$vTx(ild,ild1,y)..
```

```
LOSS(ild,ild1,y,t,blk) =g=
```

```
intercept(ild,ild1,y,n) + slope(ild,ild1,y,n) *TX(ild,ild1,y,t,blk) ;
```

- A more complex formulation was trialed using SOS2 variables
 - Has the advantage that it works with non-convex functions (not an issue with transmission losses), and min or max objective functions
 - Seemingly high computational overhead, i.e. ~1000 SOS2 sets each with 6 members, but solved in similar time to simple formulation using CPLEX

Losses – cont'd



Security constraints

** Ensure enough NZ available peak capacity to meet NZ peak.*

```
bal_security_NZ(vY(y))$UseSecurityCon..  
SUM(s, CAPACITY(s,y) * peakcontribution(s) ) -  
largestNIGen(y) - largestSIGen(y) - NxtLrgstNIGen(y) -  
freqKeepNI(y) - freqKeepSI(y) -  
maxTxLosses(y) * txcap('si','ni',y) + NZSECURITYSLACK(y)  
=g= peakload(y,'NZ_peak') ;
```

** Ensure enough NI available peak capacity to meet NI peak demand, considering HVDC losses.*

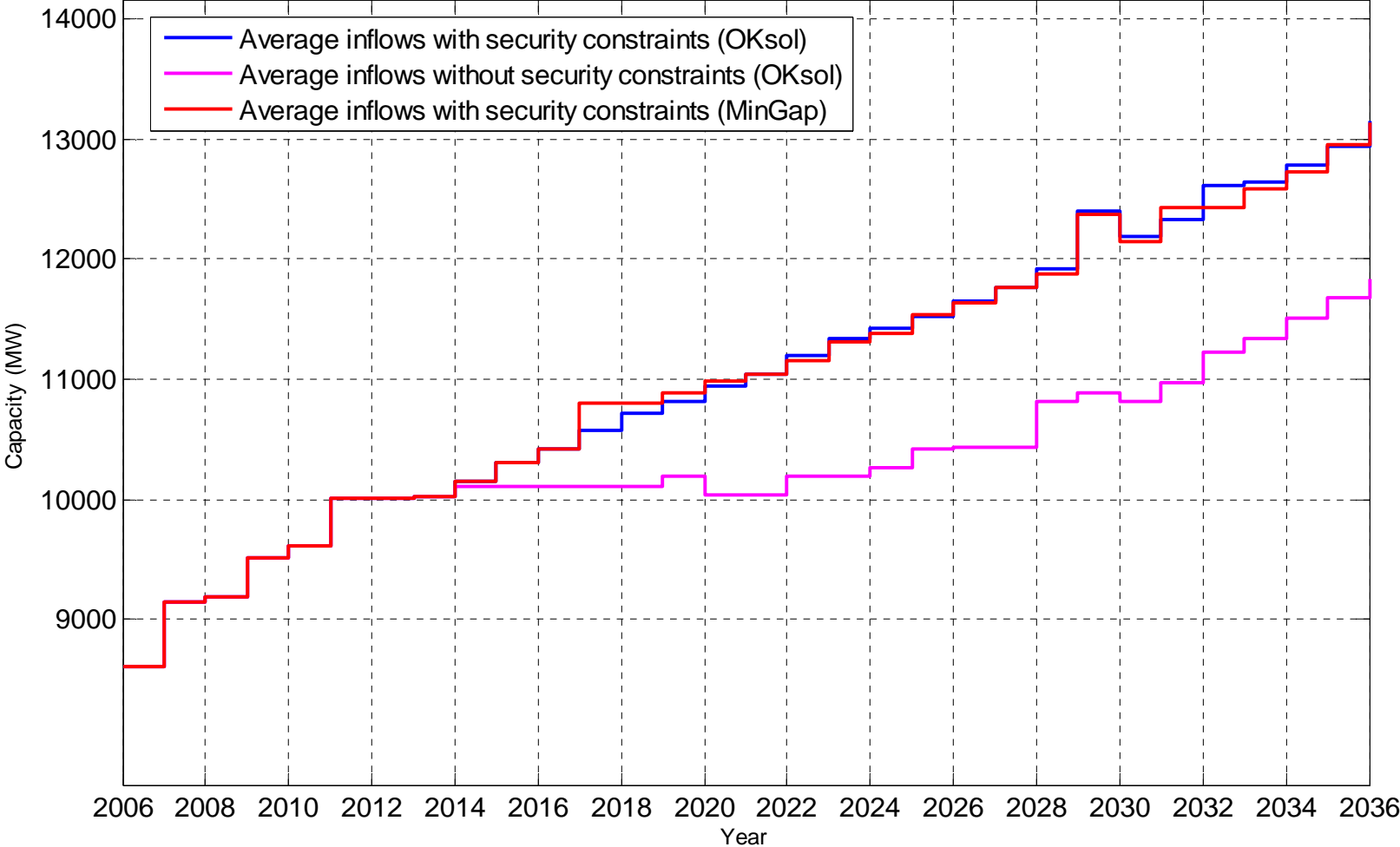
```
bal_security_NI1(vY(y))$UseSecurityCon..  
SUM(nigen(s), CAPACITY(s,y) * peakcontribution(s) ) -  
largestNIGen(y) - NxtLrgstNIGen(y) - freqKeepNI(y) +  
txcap('si','ni',y) * (1 - maxTxLosses(y)) + NI1SECURITYSLACK(y)  
=g= peakload(y,'NI_peak') ;
```

** Ensure enough capacity to meet NI peak demand if one pole is out.*

```
bal_security_NI2(vY(y))$UseSecurityCon..  
SUM(nigen(s), CAPACITY(s,y) * peakcontribution(s) ) -  
largestNIGen(y) - freqKeepNI(y) +  
txcapPo('si','ni',y) * (1 - maxTxLossesPO(y)) + NI2SECURITYSLACK(y)  
=g= peakload(y,'NI_peak') ;
```


Build schedule, mds1

Installed capacity - High gas discovery (mds1)

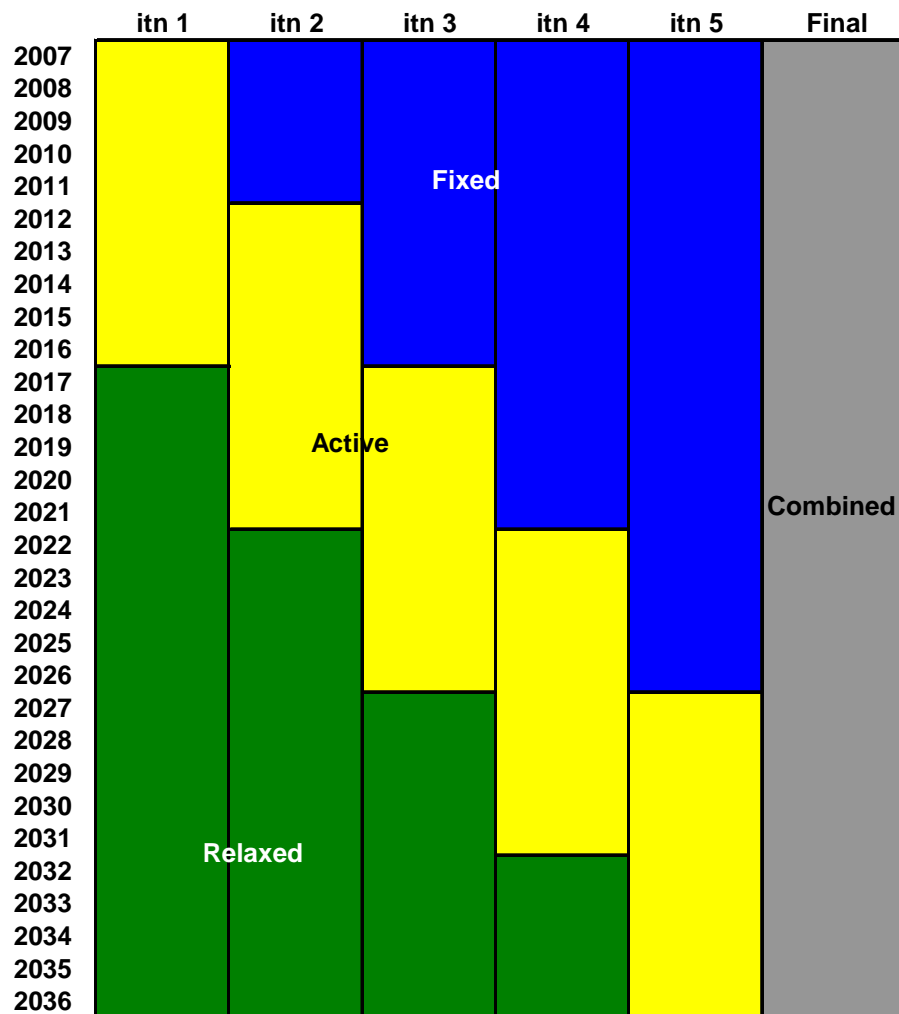


One or two contentious topics

- Revenue and/or generation adequacy?
- Least cost (central planner) v market behaviour?
 - Australian 'GIT' requires a least cost expansion plan...
- Implied market design?
 - Energy and/or capacity, or both
- Implied prices
 - Energy prices are straightforward
 - Capacity prices are complicated

Solution strategies

- QDsol – quick and dirty
 - Entire horizon
- OKsol – obtain o.k. solutions
 - Entire horizon
 - Rolling horizon
- MinGap – prove optimality
 - Entire horizon
 - Rolling horizon

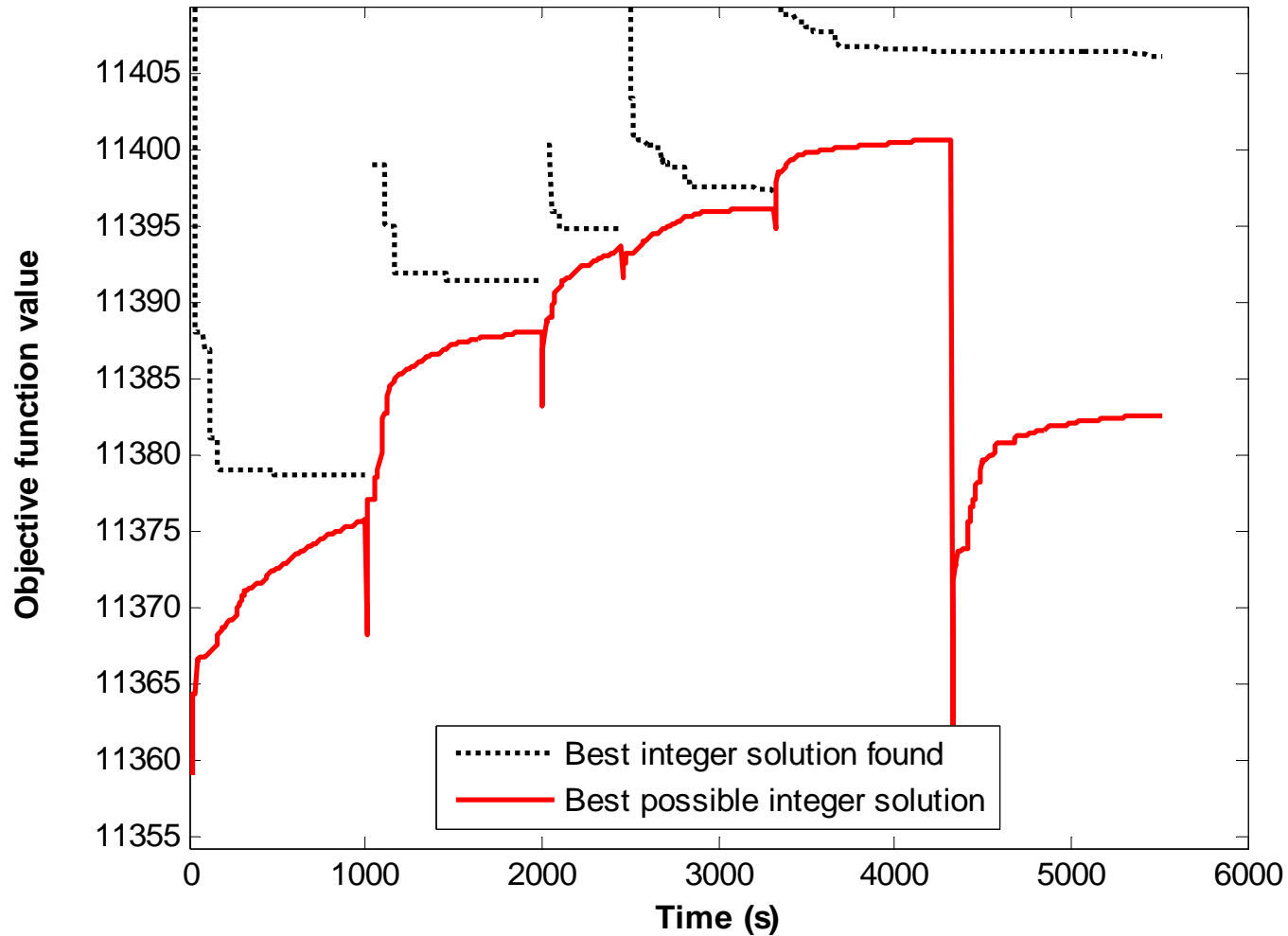


Solution strategies compared, mds3

		Actual	Best	Gap	Gap%	Secs	# bin vars	Options
Oksol (rolling horizon)	ltn 1	11,378.8	11,375.8	3.0	0.03	1,000	371	2
	ltn 2	11,391.5	11,388.1	3.4	0.03	1,000	748	3
	ltn 3	11,394.8	11,393.7	1.1	0.01	453	894	3
	ltn 4	11,397.3	11,396.2	1.1	0.01	869	1,000	3
	ltn 5	11,406.5	11,400.7	5.8	0.05	1,000	1,121	3
	Final	11,406.2	11,382.6	23.6	0.21	<u>1,200</u>	2,386	4
						5,522		
OKsol (entire)	Final	11,408.5	11,382.2	26.2	0.23	5,000	2,386	6
MinGap	ltn 1	11,378.7	11,375.8	2.9	0.03	1,000	371	2
	ltn 2	11,391.3	11,387.8	3.5	0.03	1,000	748	3
	ltn 3	11,394.6	11,393.5	1.1	0.01	402	894	3
	ltn 4	11,397.2	11,396.0	1.1	0.01	819	1,000	3
	ltn 5	11,405.7	11,400.7	4.9	0.04	1,000	1,121	3
	Final	11,405.5	11,391.2	14.3	0.13	<u>7,200</u>	2,386	5
						11,421		
QDsol (entire)	Final	11,468.2	11,377.8	90.4	0.79	261	2,386	8

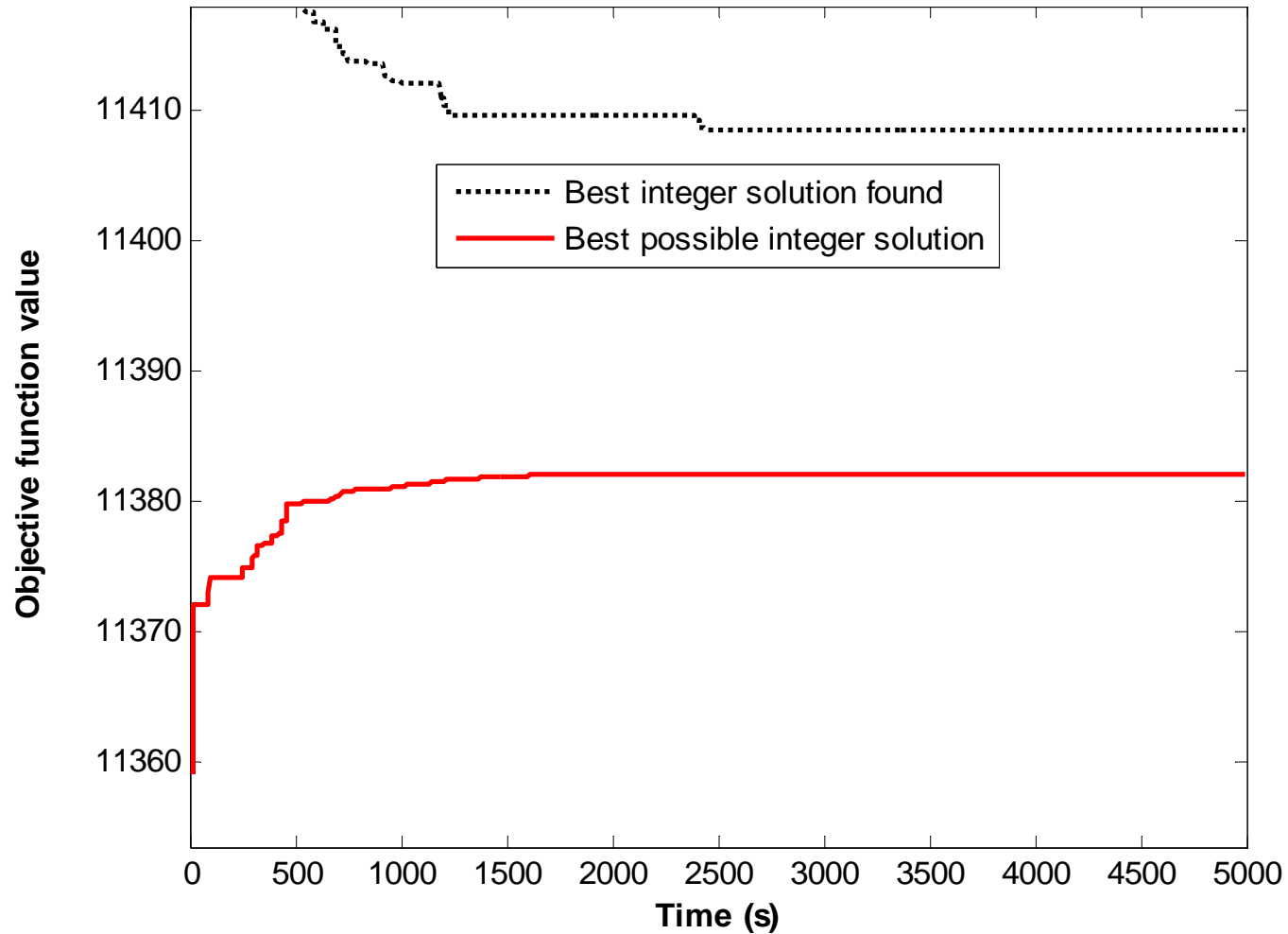
Solution trace, OKsol, rolling horizon (mds3)

Combined CPLEX trace plot

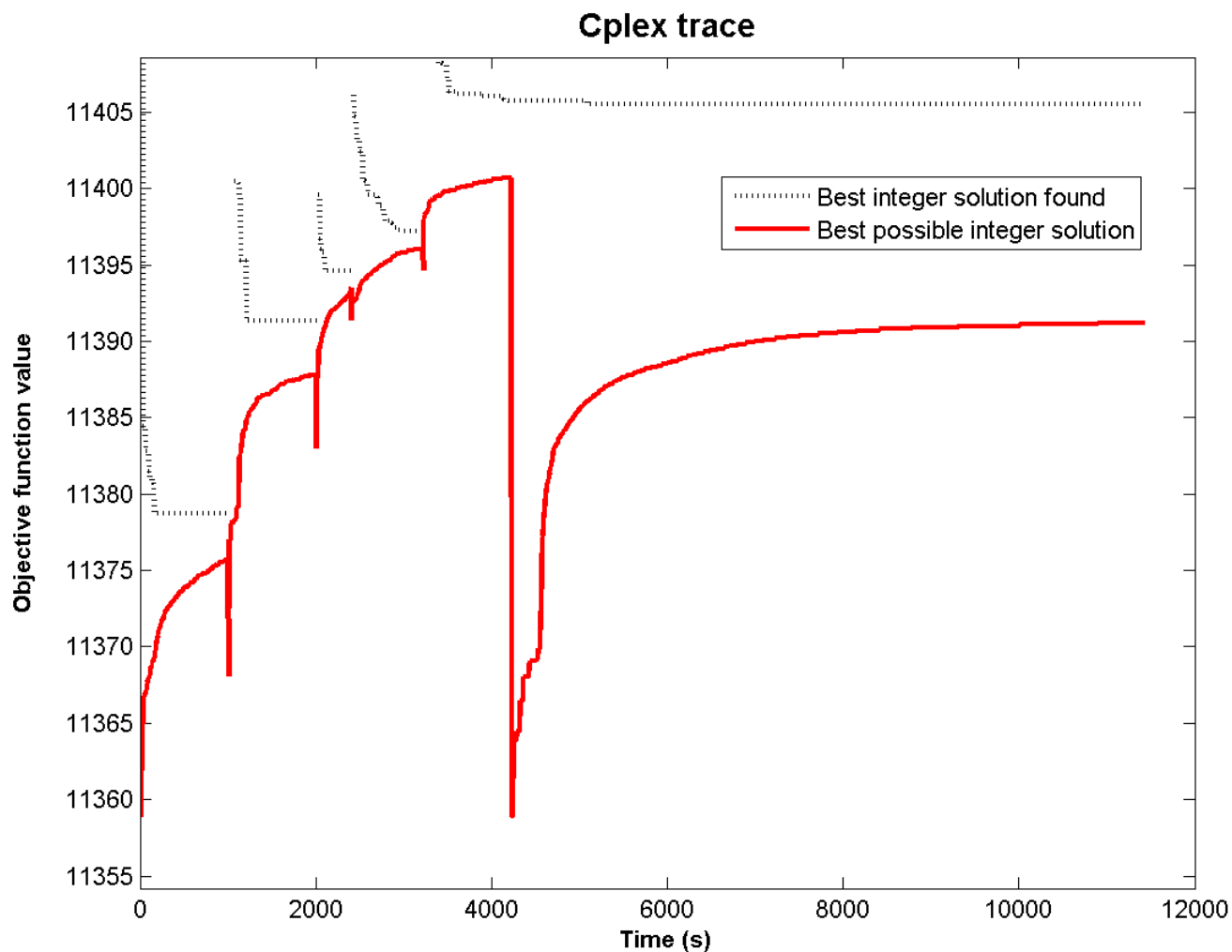


Solution trace, OKsol, entire horizon (mds3)

CPLEX trace plot

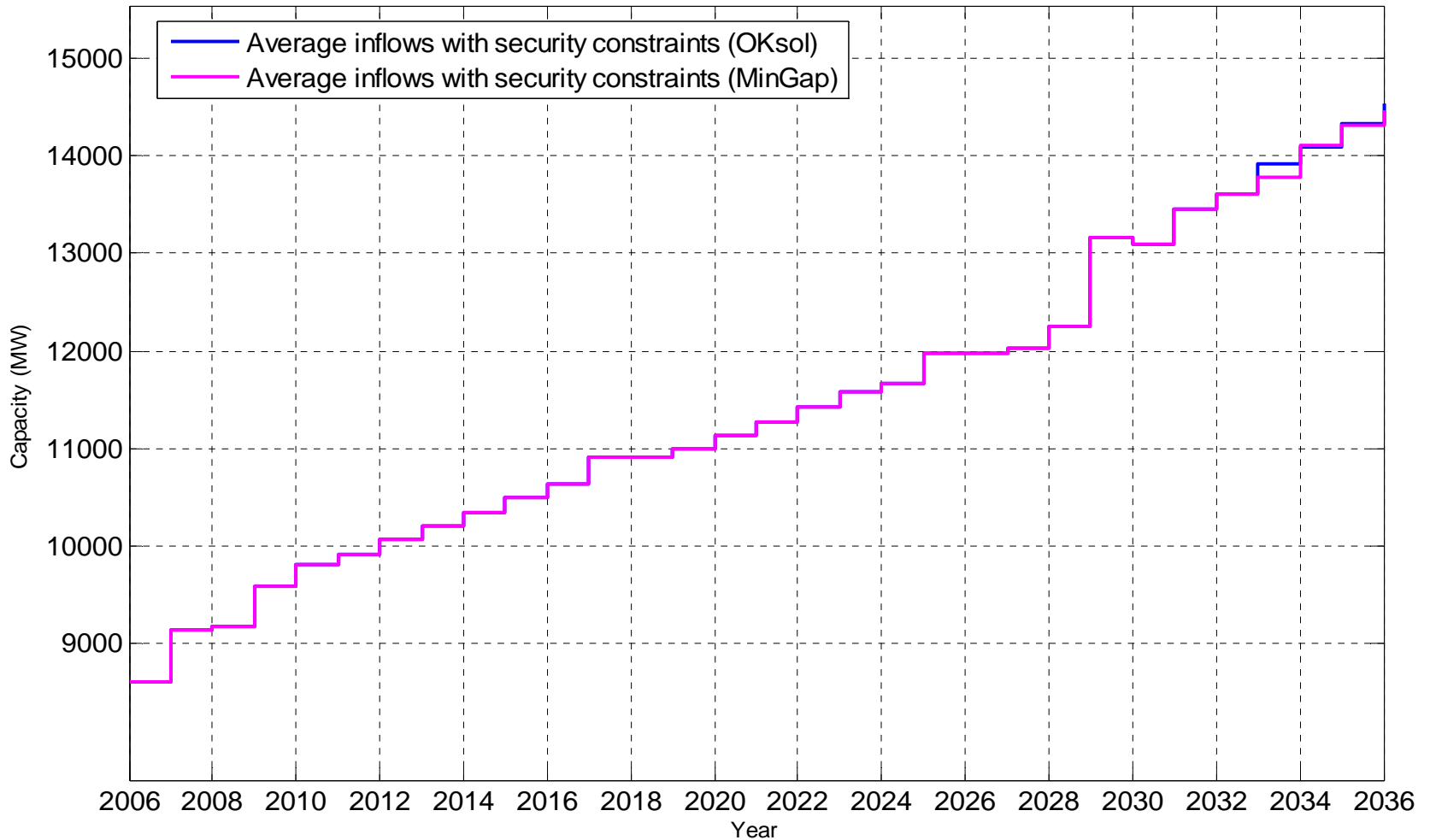


Solution trace, MinGap (mids3)



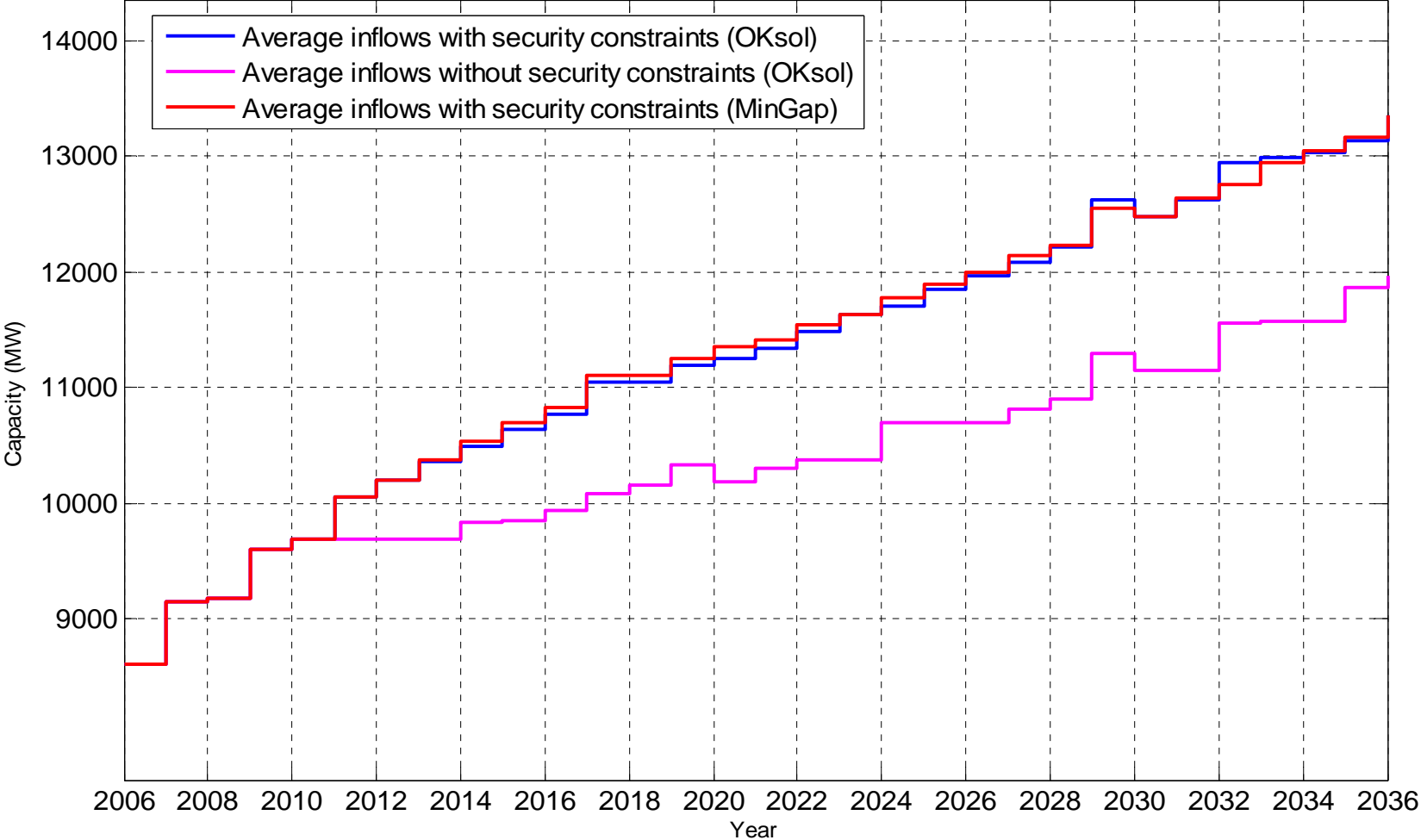
Build schedule, mds3

Installed capacity - Primary renewables (mds3)



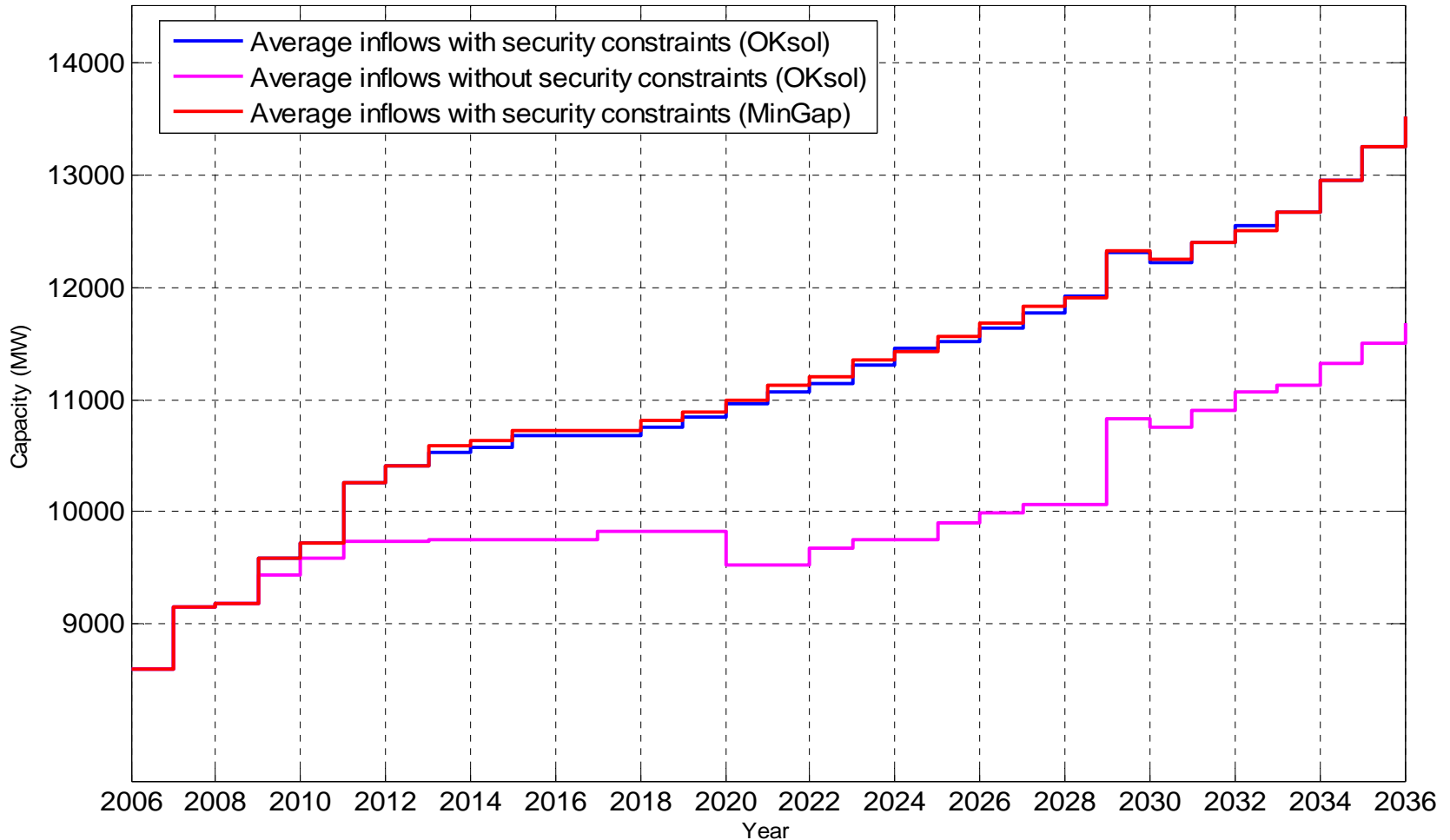
Build schedule, mds2

Installed capacity - Mixed technologies (mds2)

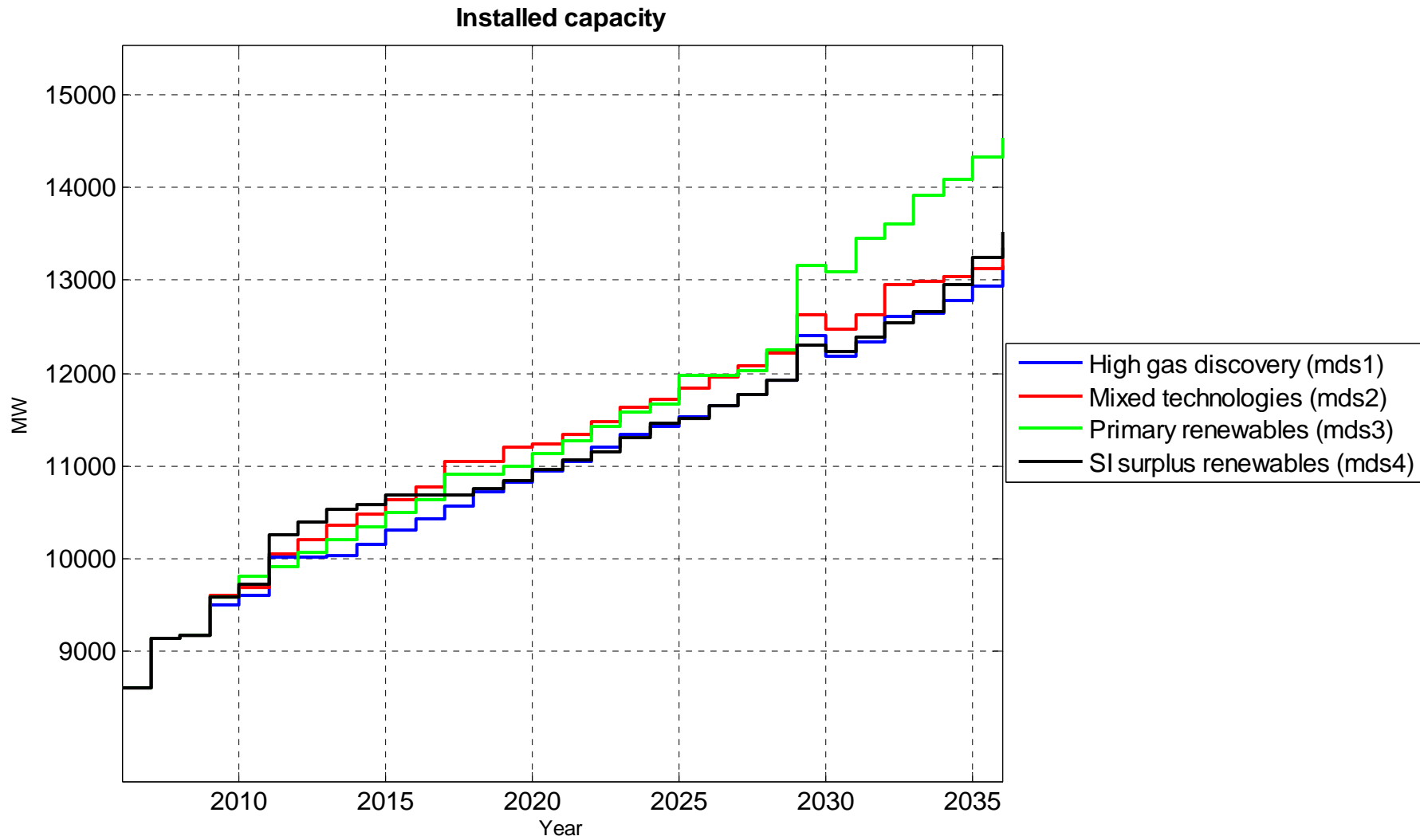


Build schedule, mds4

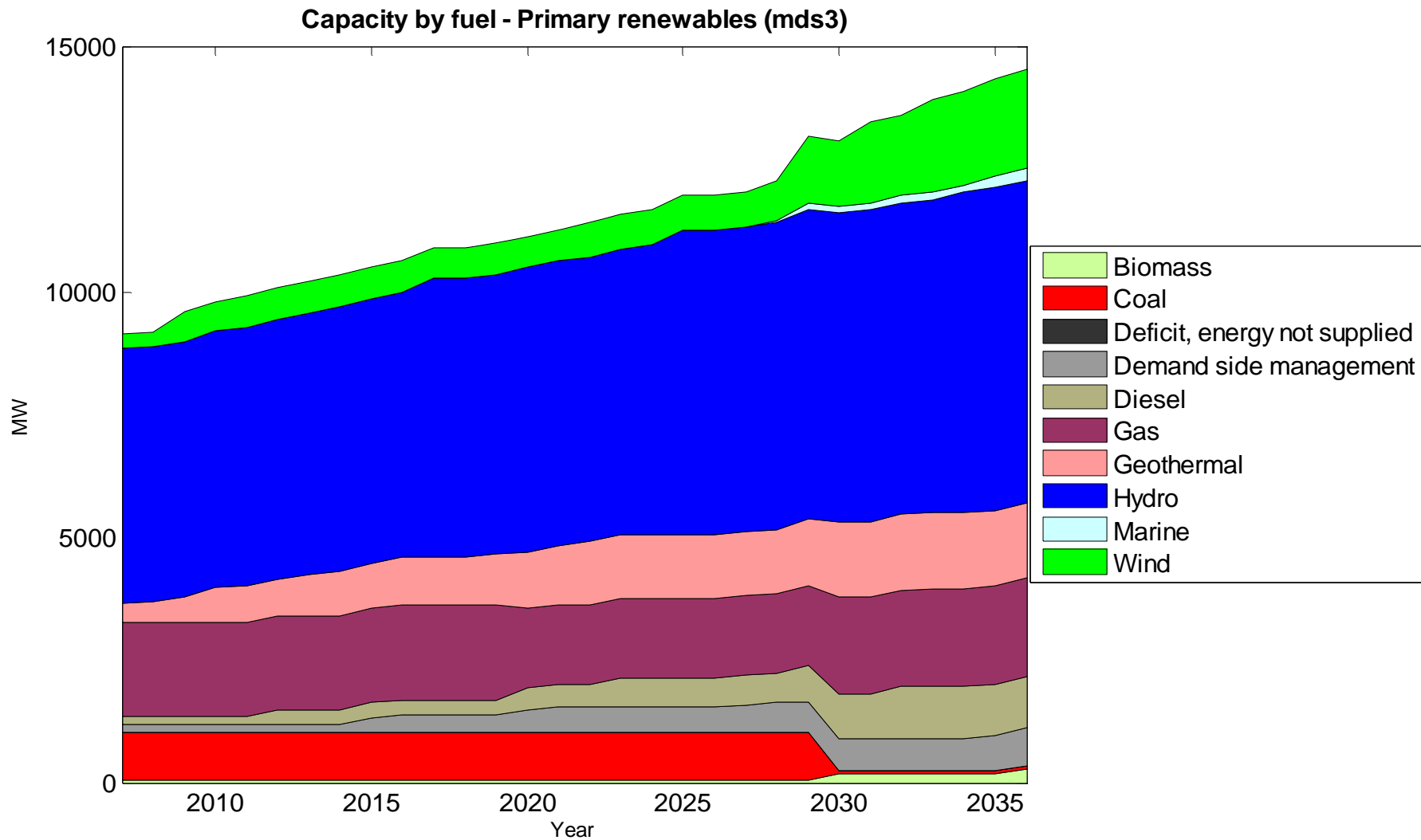
Installed capacity - South Island surplus renewables (mds4)



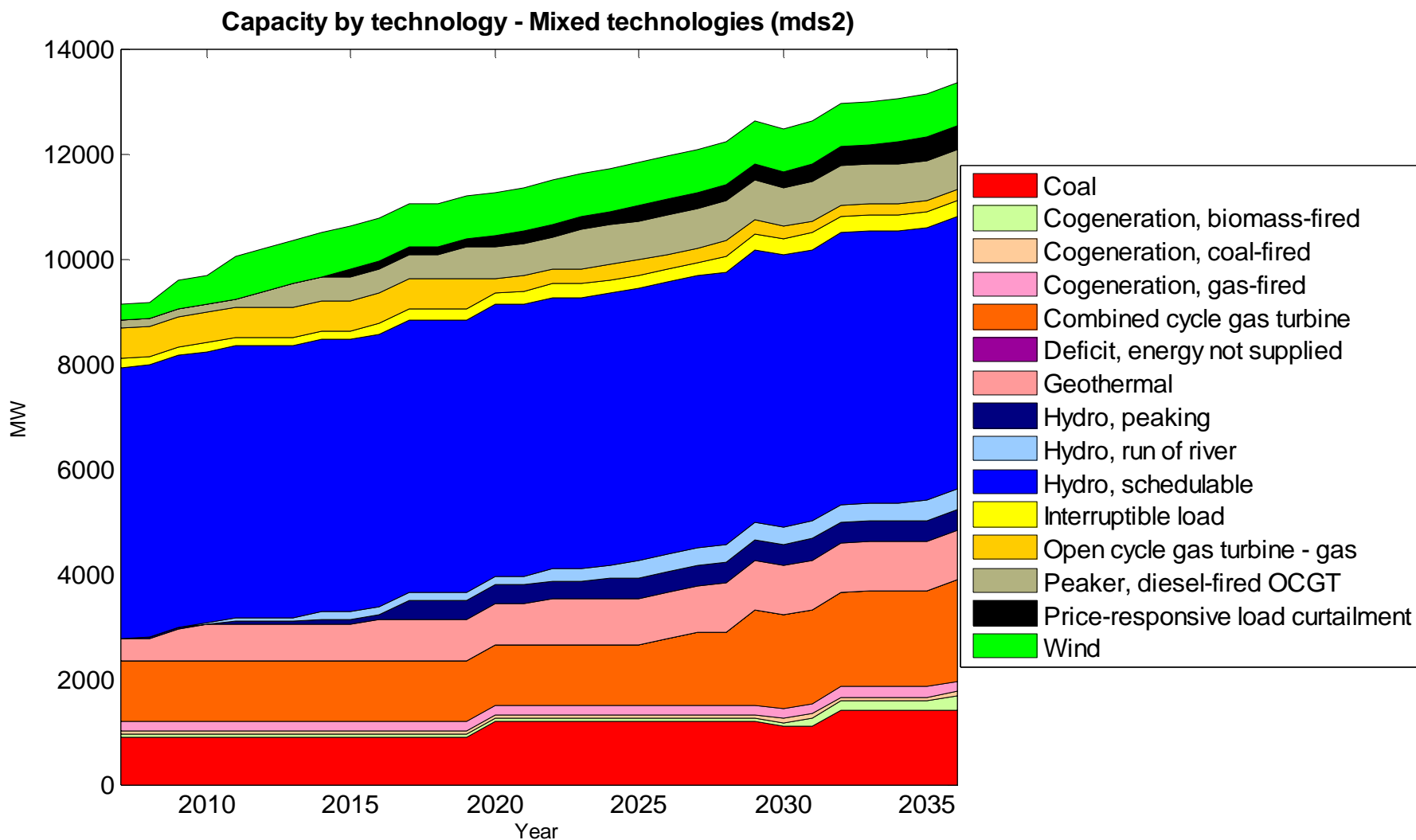
GEM outputs – build schedule



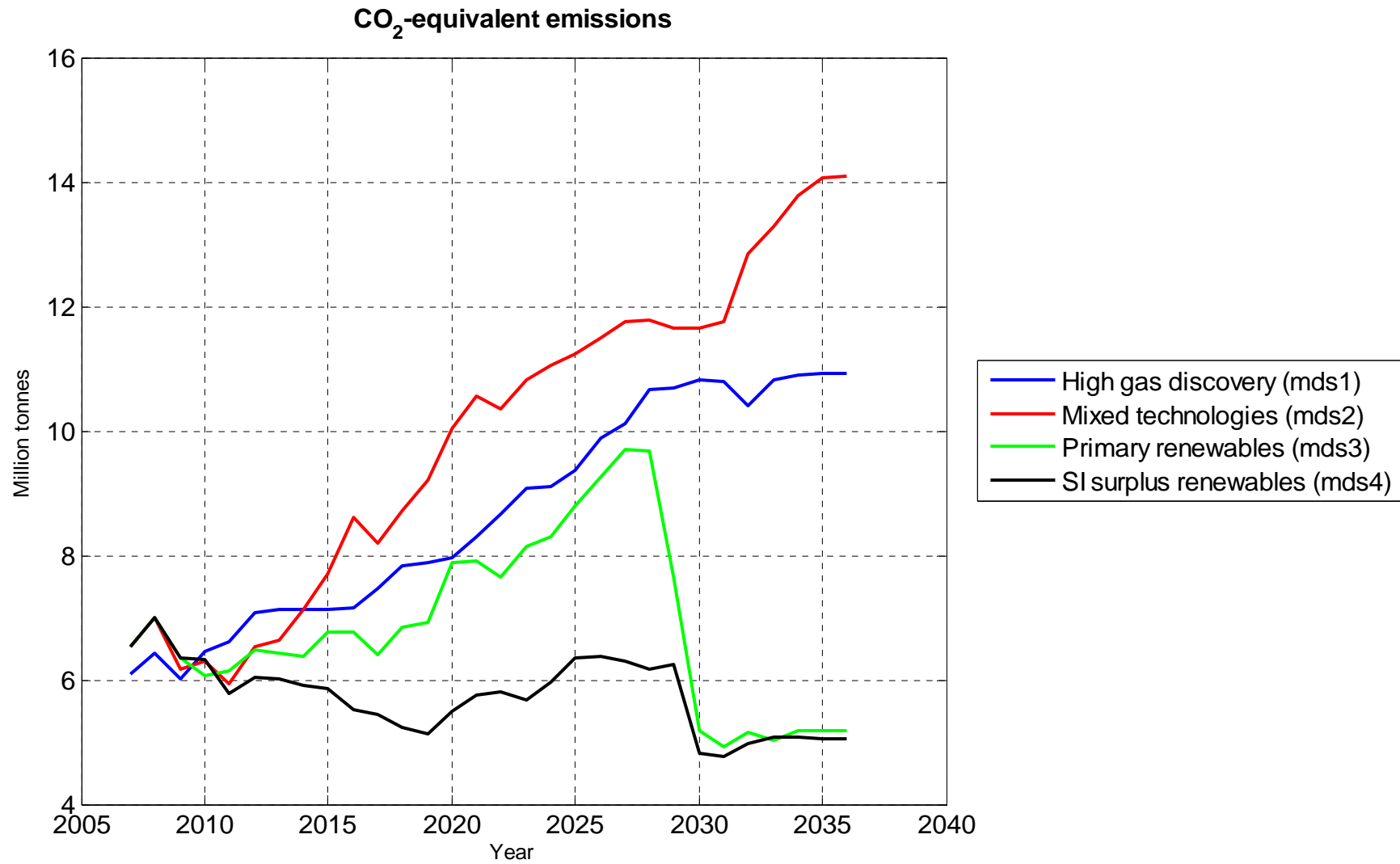
GEM outputs – capacity by fuel type



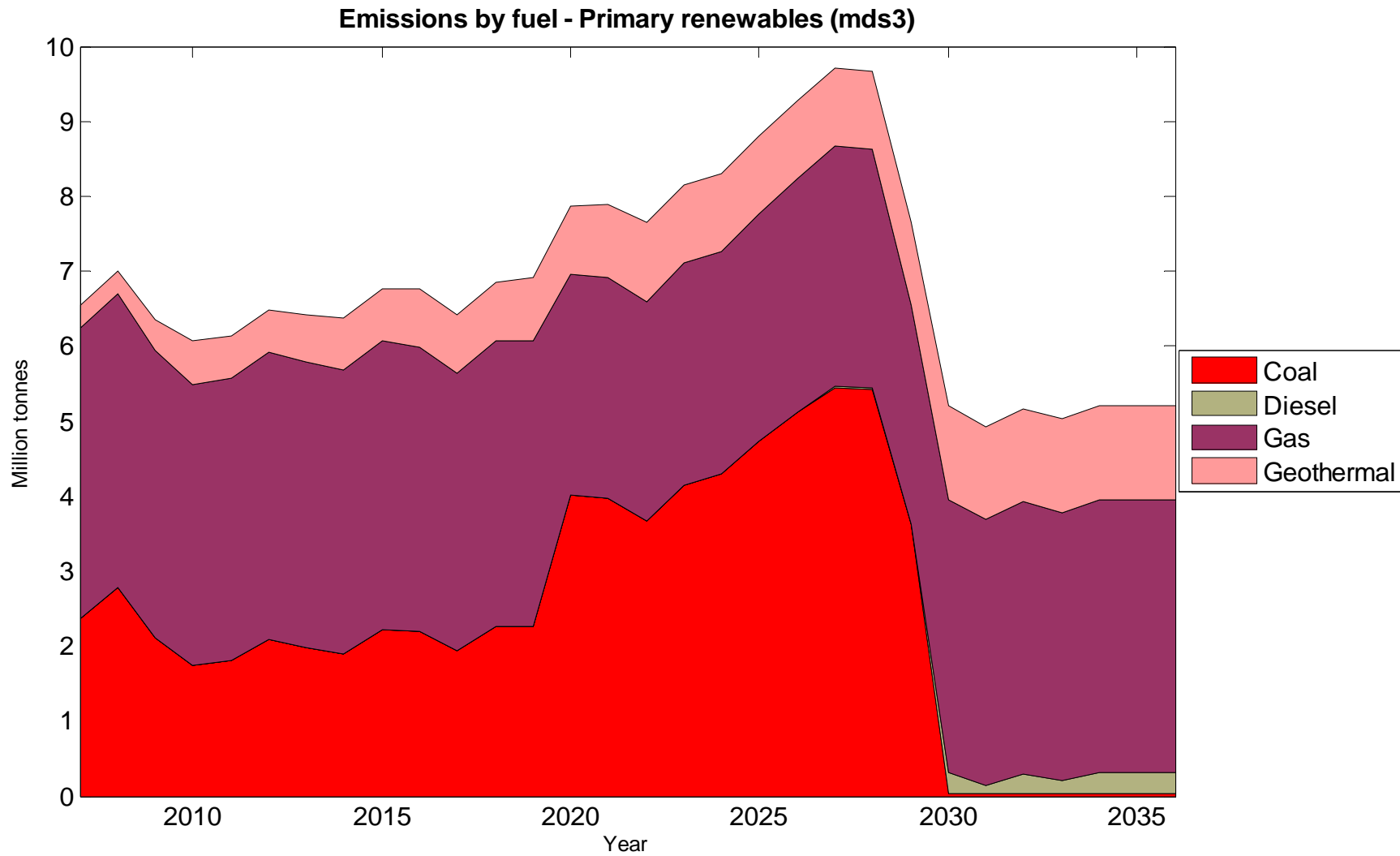
GEM outputs – capacity by technology type



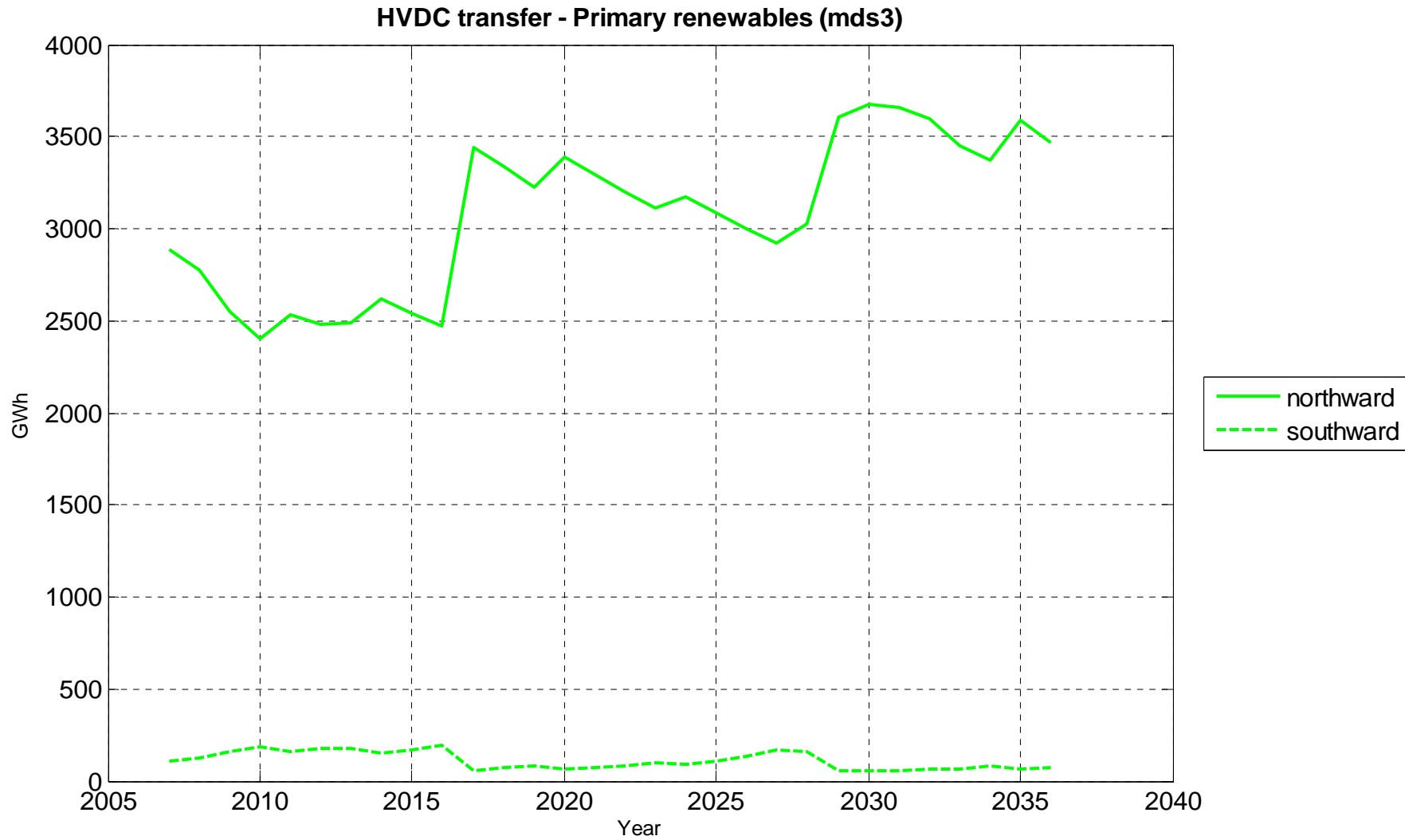
GEM outputs – CO₂-equivalent emissions



GEM outputs – emissions by fuel type



GEM outputs – HVDC transfer



What next?

- Validation against similar models
- Finish preparing documentation and user manual
- Endogenise transmission investment, i.e. co-optimize with generation investment
- 19 regions with interregional transmission (currently 2 nodes)
- Monthly, 5-block load duration curve (currently quarterly 4-block LDC)
- Rethink HVDC/Tx pricing
- Hydro storage with intertemporal management of hydro resource
 - Perhaps some simple rules to mimic water valuation, but no intention to implement a stochastic treatment of inflow uncertainty

Further information

<http://www.electricitycommission.govt.nz/opdev/modelling/gem/index.html>

or email gem@electricitycommission.govt.nz